

Analyzing dose-volume histograms using DVHmetrics for R

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July 29, 2016

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1 Introduction

DVHmetrics is an add-on package for the free statistical environment R¹ (R Development Core Team, 2015) with applications in radiation oncology. It provides functionality to read dose-volume-histogram (DVH) text files, to calculate DVH metrics, and to plot DVHs. In addition, it checks and visualizes quality assurance constraints for the DVH.²

To install DVHmetrics, you need a current version of R and be online. Preferably, a free development environment like RStudio (RStudio Inc, 2015) or Architect (OpenAnalytics BVBA, 2015) should be used.

```
# install DVHmetrics from the CRAN online package repository
install.packages("DVHmetrics")
```

2 Interfaces

DVHmetrics provides two interfaces geared towards users with different levels of familiarity with R: The regular command line functions and a built-in web application.

2.1 R command line interface

Users familiar with R can use the DVHmetrics package functions from the R command line. This facilitates statistical post-processing of results with the full capabilities of R. After installing DVHmetrics, you should be able to run (function `getMetric()` is explained in section 4.1):

```
## load DVHmetrics package - required for all following tasks
library(DVHmetrics, verbose=FALSE)

## calculate a DVH metric for built-in data
getMetric(dataMZ, metric="DMEAN", structure="HEART")
```

	observed	metric	structure	patID
1	18.110	DMEAN	HEART	P123
2	0.995	DMEAN	HEART	P234
3	10.389	DMEAN	HEART	P345

2.2 Web-based graphical user interface

For users who are unfamiliar with R, DVHmetrics includes a shiny-based web application (RStudio Inc., 2015) running locally that eliminates the need to use R syntax. For information on how to use this app, see the documentation by running this from the command line:

¹Free short introductions to R can be found at

<http://www.splusebook.com/RIntro/RCourse.pdf> and <http://www.statmethods.net/>.

²For a solution that also reads files in DICOM-RT format, see the RadOnc package for R (Thompson, 2015).

```
vignette("DVHshiny")
```

3 Read DVH text data

To import DVH data into R, it should be exported as a plain text file from Varian Eclipse™ (Versions 8–13), CadPlan™, Pinnacle³™ (version 9³), Oncentra MasterPlan™ (version 4.3), Elekta Monaco™ (version 5), TomoTherapy HiArt™, or from RaySearch Labs RayStation™. DVH files from different TPSs can be combined into one set of DVHs. Cumulative and differential DVHs are supported, as are sum plans. The measurement unit for absolute dose can be Gy or cGy, the measurement unit for volume has to be cm³. Multiple DVH text files can be read with `readDVH()` in one step.

Example: Read one Eclipse file `dvhFile.txt` from folder `"c:/folder"` and save the result in object `res`.⁴

```
res <- readDVH("c:/folder/dvhFile.txt", type="Eclipse")
```

Basic information about the files can be displayed with `print()`, or just by entering the name of a DVH object at the prompt – here used with built-in DVHs from three patients with radiotherapy, each with seven heart structures.⁵

```
print(dataMZ)
```

DVH list of 3 lists - 1 for each patient:

DVH list:

Patient 'John Doe' (ID P123, prescription dose 60GY) with 7 Structures:
HEART, AOVALVE, AMYOCR, PULMVALVE, MYOCARD, AMYOCL, AVNODE

DVH list:

Patient 'Jane Doe' (ID P234, prescription dose 60GY) with 7 Structures:
AMYOCR, AVNODE, HEART, AOVALVE, PULMVALVE, MYOCARD, AMYOCL

DVH list:

Patient 'Jane Smith' (ID P345, prescription dose 60GY) with 7 Structures:
HEART, AOVALVE, PULMVALVE, MYOCARD, AMYOCL, AMYOCR, AVNODE

Display more information on structures with `verbose=TRUE`.

³Pinnacle³ files have to be exported such that information from one patient is contained in one directory. The directory layout and required files are explained in `help(readDVH)`.

⁴Note that the way to indicate the path to these files is different from the usual Windows style path: Instead of writing the backslash "\" as folder separator, the forward slash "/" must be used.

⁵Sample data courtesy of Department of Radiation Oncology (Prof. Dr. Schmidberger), University Medical Center Mainz, Germany.

```
print(dataMZ, verbose=TRUE)
```

DVH list of 3 lists - 1 for each patient:

DVH list:

Patient 'John Doe' (ID P123, prescription dose 60GY) with 7 Structures:

DVH: Structure 'HEART' (600 CC), Dose: 0-62GY
DVH: Structure 'AOVALVE' (12 CC), Dose: 0-62GY
DVH: Structure 'AMYOCR' (57 CC), Dose: 0-62GY
DVH: Structure 'PULMVALVE' (3.8 CC), Dose: 0-62GY
DVH: Structure 'MYOCARD' (310 CC), Dose: 0-62GY
DVH: Structure 'AMYOCL' (60 CC), Dose: 0-62GY
DVH: Structure 'AVNODE' (38 CC), Dose: 0-62GY

DVH list:

Patient 'Jane Doe' (ID P234, prescription dose 60GY) with 7 Structures:

DVH: Structure 'AMYOCR' (53 CC), Dose: 0-63GY
DVH: Structure 'AVNODE' (43 CC), Dose: 0-63GY
DVH: Structure 'HEART' (730 CC), Dose: 0-63GY
DVH: Structure 'AOVALVE' (15 CC), Dose: 0-63GY
DVH: Structure 'PULMVALVE' (6.7 CC), Dose: 0-63GY
DVH: Structure 'MYOCARD' (330 CC), Dose: 0-63GY
DVH: Structure 'AMYOCL' (81 CC), Dose: 0-63GY

DVH list:

Patient 'Jane Smith' (ID P345, prescription dose 60GY) with 7 Structures:

DVH: Structure 'HEART' (550 CC), Dose: 0-62GY
DVH: Structure 'AOVALVE' (11 CC), Dose: 0-62GY
DVH: Structure 'PULMVALVE' (5.7 CC), Dose: 0-62GY
DVH: Structure 'MYOCARD' (270 CC), Dose: 0-62GY
DVH: Structure 'AMYOCL' (43 CC), Dose: 0-62GY
DVH: Structure 'AMYOCR' (52 CC), Dose: 0-62GY
DVH: Structure 'AVNODE' (24 CC), Dose: 0-62GY

Multiple files with the same name pattern can be specified using wildcards like *. Example: Read all CadPlan files with the file name pattern `dvhFile*.txt` from folder `"c:/folder"` and save the result in object `res`.

```
res <- readDVH("c:/folder/dvhFile*.txt", type="Cadplan")
```

When no file pattern is specified, multiple files can be selected using the standard Windows file picker dialogue. On MacOS and Linux, only a single file can be selected interactively.

```
res <- readDVH(type="Eclipse") # opens interactive file picker
```

For DVH files from a sum plan, prescribed dose can be encoded in the plan name like `name_70Gy_etc`. It will then be assumed that “% for dose” is 100.

```
res <- readDVH("c:/folder/*", type="Eclipse", planInfo="doseRx")
```

4 DVH metrics

4.1 Calculate DVH metrics

Function `getMetric()` calculates freely-defined DVH metrics based on data that has been read in as demonstrated in section 3. `getMetric()` has the following options:

- Option `x`: The DVH data.
- Option `metric` – one or many of the following:
 - A *pre-specified* DVH metric is one of the following character strings:
 - * "DMEAN": The volume-weighted mean dose of the structure.
 - * "DMIN": The minimum dose of the non-zero-dose voxels in the structure.
 - * "DMAX": The maximum dose of the non-zero-dose voxels in the structure.
 - * "DSD": The standard deviation of the dose in the structure.
 - * "DRX": The prescription dose.
 - * "DHI": The Homogeneity Index according to ICRU 83: $(D2\%-D98\%)/D50\%$.
 - * "DEUD": The generalized equivalent uniform dose (gEUD, Niemierko, 1999; Wu, Mohan, Niemierko, & Schmidt-Ullrich, 2002). This can be based on EQD₂ values if information on the fractionation is provided as well (IAEA & ICRU, 2008).
 - * "DNTCP": The normal tissue complication probability (NTCP) according to the Lyman (1985) probit model, the Niemierko (1999) logit model, or the Poisson model (equation (3) in Källman, Ågren, & Brahme, 1992 with gEUD plugged in for D). This can be based on EQD₂ values if information on the fractionation is provided as well.
 - * "DTCP": The tumor control probability (TCP) according to the same models as NTCP.
 - A *free* DVH metric is a character string which has three mandatory elements and one optional element in the following order:
 - * 1st letter "D" or "V": "D" If the requested value is a dose, "V" if it is a volume.
 - * 2nd element `<number>`: If the first letter is "D", this gives the volume for which the dose value of the cumulative DVH should be reported. If the first letter is "V", this gives the dose for which the volume value of the cumulative DVH should be reported.
 - * 3rd element `<measurement unit>`: The measurement unit for the 2nd element of the metric. Absolute volumes are indicated by "CC" for cm³, relative volumes by "%". Absolute doses are indicated by "Gy" for Gray or "cGy" for Centigray, relative doses by "%".
 - * Optional 4th element `_<measurement unit>`: The measurement unit of the output value. Possible units are the same as for the 3rd element. If missing, dose is reported as absolute dose in the measurement unit used in the DVH. If the measurement unit is missing, volume is reported as relative volume in %.

- Example metrics are listed in table 1. By default, metrics are calculated using linear interpolation between adjacent supporting points of the cumulative DVH – without extrapolating beyond the observed volume or dose. The interpolation method can be changed to use monotone Hermite splines (Fritsch & Carlson, 1980), or to local polynomial regression with a Gaussian kernel (Wand & Jones, 1995). The kernel bandwidth is then determined by the direct plug-in method (Ruppert, Sheather, & Wand, 1995).
- Option **patID**: Which patient IDs should be analyzed. With **fixed=FALSE**, IDs are interpreted as regular expressions matched against those found in the DVH files. By default, IDs are matched exactly. If missing, the metrics are calculated for all patients.
- Option **structure**: Which structure should be analyzed. With **fixed=FALSE**, structure names are interpreted as regular expressions matched against those found in the DVH files. By default, structure names are matched exactly. If missing, the metrics are calculated for all structures.
- Option **sortBy**: Results can be sorted according to these variables:
 - "observed": observed value of the metric
 - "structure": structure for which the metric is calculated
 - "metric": type of calculated metric
 - "patID": patient ID
- Option **splitBy**: Results can be divided into different tables according to these variables:
 - "structure": structure for which the metric is calculated
 - "metric": type of calculated metric
 - "patID": patient ID

Table 1: Examples of possible DVH metrics

Metric	Reference	Unit reference	Result	Unit result
"V10Gy"	absolute dose	Gy	relative volume	%
"V10cGy_CC"	absolute dose	cGy	absolute volume	cm ³
"V10%"	relative dose	%	relative volume	%
"V10%_CC"	relative dose	%	absolute volume	cm ³
"D10CC"	absolute volume	cm ³	absolute dose	as in DVH
"D10%_cGy"	relative volume	%	absolute dose	cGy
"DMEAN"	—	—	absolute dose	as in DVH
"DEUD"	—	—	absolute dose	as in DVH
"DSD"	—	—	absolute dose	as in DVH
"DMIN"	—	—	absolute dose	as in DVH
"DMAX"	—	—	absolute dose	as in DVH
"DHI"	—	—	dose ratio	—
"DNTCP"	—	—	probability	—
"DTCP"	—	—	probability	—

If volume or dose values outside the range of possible values for a structure are requested, it may be that metrics cannot be calculated, and the result will be NA (missing value) with a warning.

In the following examples, we use object `dataMZ` that is built into the `DVHmetrics` package. `dataMZ` was the result from reading three Eclipse DVH files, each with seven structures – as demonstrated in section 3.

Calculate metric DMEAN for all structures for all patients in `dataMZ`.

```
getMetric(dataMZ, metric="DMEAN")
```

	observed	metric	structure	patID
1	18.110	DMEAN	HEART	P123
2	21.454	DMEAN	AOVALVE	P123
3	24.046	DMEAN	AMYOCR	P123
4	23.015	DMEAN	PULMVALVE	P123
5	17.492	DMEAN	MYOCARD	P123
6	18.496	DMEAN	AMYOCL	P123
7	19.200	DMEAN	AVNODE	P123
8	2.421	DMEAN	AMYOCR	P234
9	0.968	DMEAN	AVNODE	P234
10	0.995	DMEAN	HEART	P234
11	1.959	DMEAN	AOVALVE	P234
12	1.198	DMEAN	PULMVALVE	P234
13	0.990	DMEAN	MYOCARD	P234
14	0.775	DMEAN	AMYOCL	P234
15	10.389	DMEAN	HEART	P345
16	11.283	DMEAN	AOVALVE	P345
17	10.019	DMEAN	PULMVALVE	P345
18	10.639	DMEAN	MYOCARD	P345
19	2.549	DMEAN	AMYOCL	P345
20	30.009	DMEAN	AMYOCR	P345
21	6.676	DMEAN	AVNODE	P345

Calculate metric D5cc just for structure HEART for all patients in `dataMZ`.

```
getMetric(dataMZ, metric="D5cc", structure="HEART")
```

	observed	metric	structure	patID
1	31.482	D5CC	HEART	P123
2	3.474	D5CC	HEART	P234
3	41.618	D5CC	HEART	P345

Calculate metric D5cc just for structure HEART for all patients in `dataMZ`, and sort result by the observed value of the metric.

```
getMetric(dataMZ, metric="D5cc", structure="HEART", sortBy="observed")
```

	observed	metric	structure	patID
2	3.474	D5CC	HEART	P234
1	31.482	D5CC	HEART	P123
3	41.618	D5CC	HEART	P345

Calculate metrics D10% and V5Gy for all structures containing the text AMYOC or VALVE, for patient IDs in dataMZ containing the text 23, and sort result by metric and observed value.

```
getMetric(dataMZ, metric=c("D10%", "V5Gy"),
          structure=c("AMYOC", "VALVE"),
          patID="23",
          sortBy=c("metric", "observed"),
          fixed=FALSE)
```

	observed	metric	structure	patID
15	1.312	D10%	AMYOCL	P234
13	1.404	D10%	PULMVALVE	P234
11	2.556	D10%	AOVALVE	P234
9	3.263	D10%	AMYOCR	P234
7	23.208	D10%	AMYOCL	P123
5	24.391	D10%	PULMVALVE	P123
1	25.056	D10%	AOVALVE	P123
3	30.710	D10%	AMYOCR	P123
10	0.000	V5GY	AMYOCR	P234
12	0.000	V5GY	AOVALVE	P234
14	0.000	V5GY	PULMVALVE	P234
16	0.000	V5GY	AMYOCL	P234
2	100.000	V5GY	AOVALVE	P123
4	100.000	V5GY	AMYOCR	P123
6	100.000	V5GY	PULMVALVE	P123
8	100.000	V5GY	AMYOCL	P123

Calculate metrics DMEAN and D5cc for structure HEART for all patients in dataMZ, sort by the observed value of the metric, and split the output such that one table is generated for each metric.

```
getMetric(dataMZ, metric=c("DMEAN", "D5cc"), structure="HEART",
          sortBy="observed", splitBy="metric")
```

\$D5CC

	observed	metric	structure	patID
4	3.474	D5CC	HEART	P234
2	31.482	D5CC	HEART	P123
6	41.618	D5CC	HEART	P345

\$DMEAN

	observed	metric	structure	patID
3	0.995	DMEAN	HEART	P234
5	10.389	DMEAN	HEART	P345
1	18.110	DMEAN	HEART	P123

Calculate metrics DMEAN and D5cc for structures HEART and AOVALVE for all patients in dataMZ, sort by observed value, and split the output such that one table is generated for each combination of structure and metric. Also store the result in object met that can be saved later.


```
met <- getMetric(dataMZ, metric=c("DMEAN", "D5cc"),
                 structure=c("HEART", "AOVALVE"),
                 sortBy="observed",
                 splitBy=c("structure", "metric"))
met                                     # print the calculated results
```

\$AOVALVE.D5CC

	observed	metric	structure	patID
8	2.064	D5CC	AOVALVE	P234
12	8.337	D5CC	AOVALVE	P345
4	21.752	D5CC	AOVALVE	P123

\$HEART.D5CC

	observed	metric	structure	patID
6	3.474	D5CC	HEART	P234
2	31.482	D5CC	HEART	P123
10	41.618	D5CC	HEART	P345

\$AOVALVE.DMEAN

	observed	metric	structure	patID
7	1.959	DMEAN	AOVALVE	P234
11	11.283	DMEAN	AOVALVE	P345
3	21.454	DMEAN	AOVALVE	P123

\$HEART.DMEAN

	observed	metric	structure	patID
5	0.995	DMEAN	HEART	P234
9	10.389	DMEAN	HEART	P345
1	18.110	DMEAN	HEART	P123

4.2 Save DVH metrics to file

The calculated DVH metrics can be saved to tab-delimited text files with `saveMetric()`. These files are easy to import, e. g., into spreadsheets like Excel or into other statistics programs.

Assume object `met` has been calculated before as demonstrated in section 4.1. If `met` is not split into different tables, the following command saves `met` to the file `metrics.txt`. If `met` is divided into multiple tables, this saves `met` into different files that all have the name pattern `metrics_NAME.txt`, where `NAME` stands, e. g., for the names of different structures.

```
saveMetric(met, file="c:/folder/metrics.txt")
```

Per default, numbers use the `.` as decimal separator. This can be changed with option `dec=","`.

```
saveMetric(met, file="c:/folder/metrics.txt", dec=",")
```

If text should be set in quotes in the output file, use `quote=TRUE`.

```
saveMetric(met, file="c:/folder/metrics.txt", quote=TRUE)
```

4.3 Convenience functions for DMEAN, gEUD, NTCP, TCP

DMEAN, gEUD, NTCP and TCP may be calculated together with other metrics using `getMetric()`, but there are specialized convenience functions for this task as well. In particular, `getDMEAN()` calculates the dose mean, median, mode, minimum, and maximum based on the (interpolated) differential DVH instead of relying on the values exported by the TPS.

```
dmean <- getDMEAN(dataMZ[[1]])  
subset(dmean, select=c(doseAvg, doseMed, doseMin, doseMax))
```

	doseAvg	doseMed	doseMin	doseMax
1	18.11	17.70	3.499	35.20
2	21.45	21.08	16.205	30.69
3	24.05	24.96	7.398	35.20
4	23.01	23.00	20.400	25.70
5	17.49	16.19	3.905	35.20
6	18.50	18.21	12.995	26.89
7	19.20	19.11	12.503	29.80

gEUD is calculated by `getEUD()`.

```
# note that different tissues should have different parameter values,  
# this is just for demonstration purposes  
getEUD(dataMZ[[1]], EUDa=2)
```

	EUD	patID	structure
1	18.77	P123	HEART
2	21.61	P123	AOVALVE
3	24.63	P123	AMYOCR
4	23.04	P123	PULMVALVE
5	18.33	P123	MYOCARD
6	18.77	P123	AMYOCL
7	19.35	P123	AVNODE

NTCP and TCP are calculated by `getNTCP()` and `getTCP()`, respectively.

```
# note that different tissues should have different parameter values,  
# this is just for demonstration purposes  
getNTCP(dataMZ[[1]], NTCPtd50=40, NTCPm=0.6, NTCPn=0.5, NTCPtype="probit")
```

	NTCP	patID	structure
1	0.1882	P123	HEART
2	0.2217	P123	AOVALVE
3	0.2609	P123	AMYOCR

```

4 0.2398 P123 PULMVALVE
5 0.1832 P123 MYOCARD
6 0.1882 P123 AMYOCL
7 0.1948 P123 AVNODE

```

4.4 Point-wise mean DVH with standard deviations

Function `getMeanDVH()` returns the point-wise mean and median DVH with the point-wise standard deviation for a given list of input DVHs. Other point-wise measures may be calculated as well. Before calculating the point-wise mean and SD, DVHs are first linearly interpolated such that they possess the same set of nodes. This feature can be useful for evaluating different plan options: The DVHs for each plan need to be exported using a different patient ID which thus serves as a plan identifier. See section 5.1 to show the mean DVH with SD regions.

```

# point-wise mean and SD for structure HEART over all patients
m <- getMeanDVH(dataMZ, fun=list(M=mean, SD=sd), byPat=FALSE, structure="HEART")
head(m)

```

	structure	dose	volumeM	volumeRelM	volumeSD	volumeRelSD
1	HEART	0.0	623.0	100.00	94.25	0.000
2	HEART	0.1	613.6	98.71	78.67	2.237
3	HEART	0.2	596.4	96.36	51.42	6.312
4	HEART	0.3	591.2	95.63	43.68	7.563
5	HEART	0.4	579.6	94.04	29.61	10.309
6	HEART	0.5	557.3	90.98	33.83	15.597

```

      patID
1 P123_P234_P345
2 P123_P234_P345
3 P123_P234_P345
4 P123_P234_P345
5 P123_P234_P345
6 P123_P234_P345

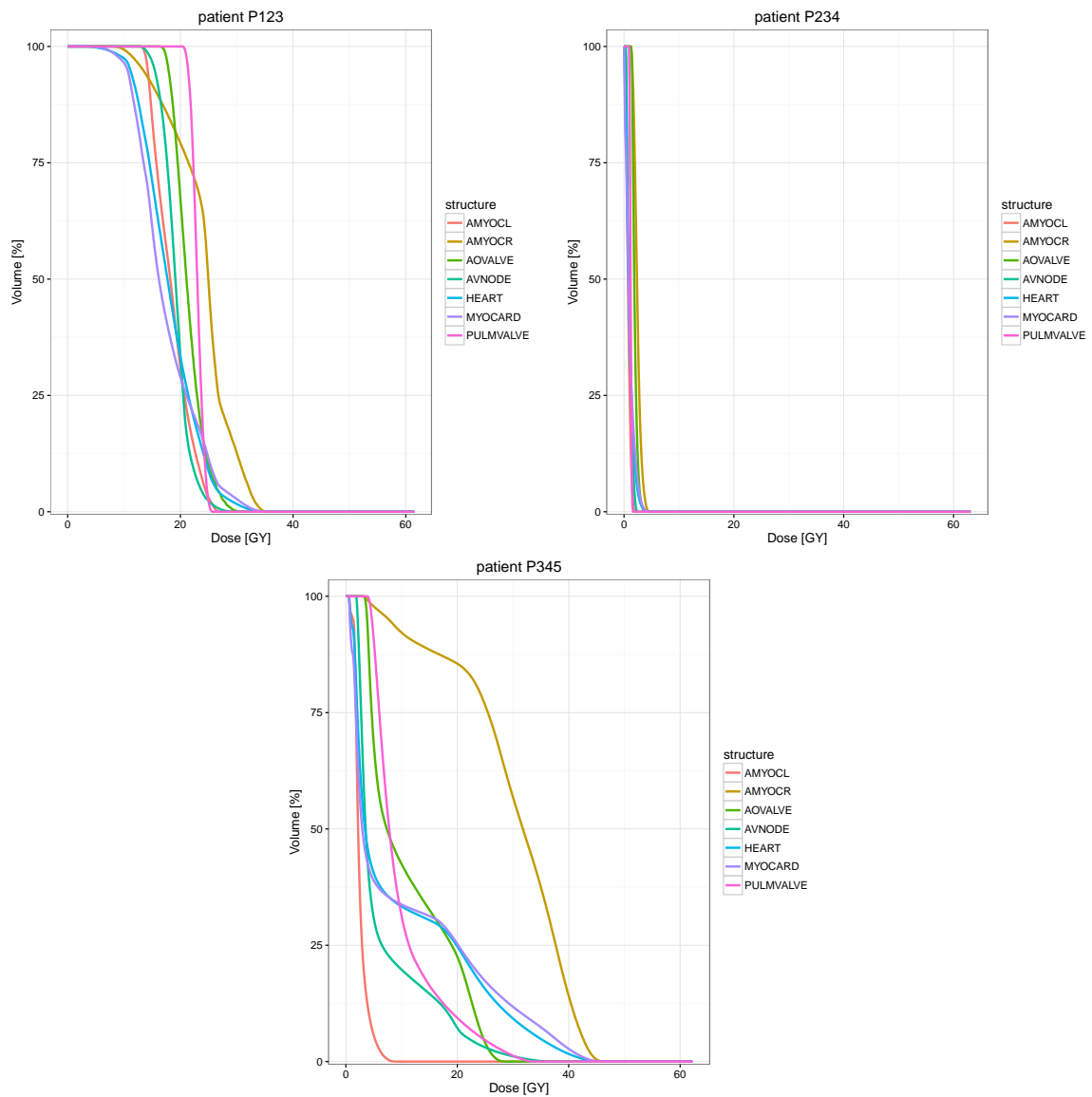
```

5 DVH diagrams

5.1 Plot DVH diagrams

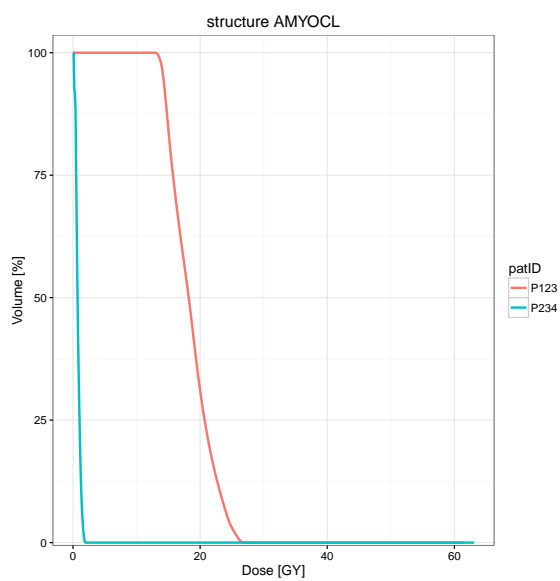
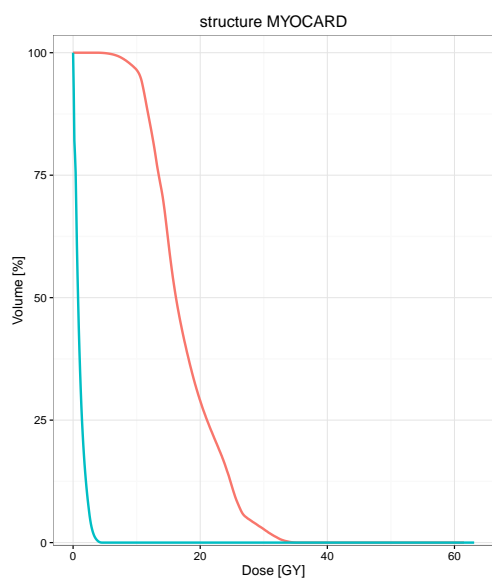
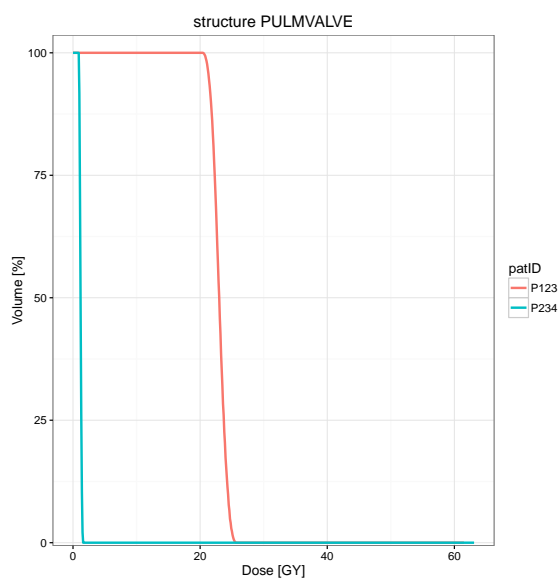
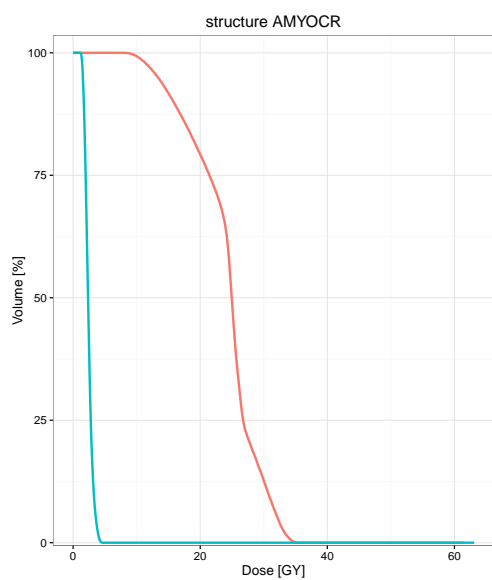
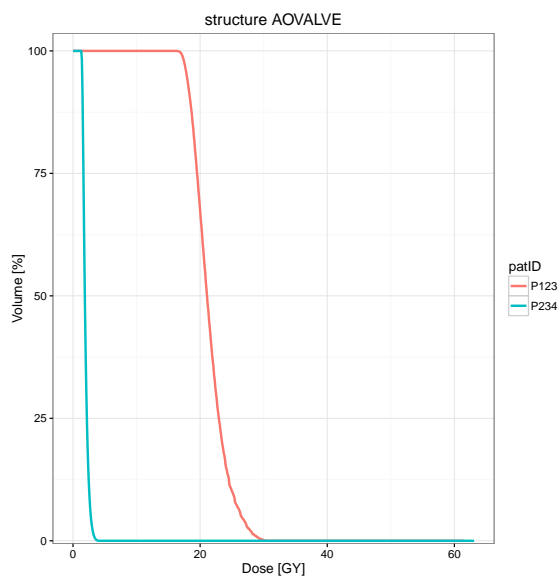
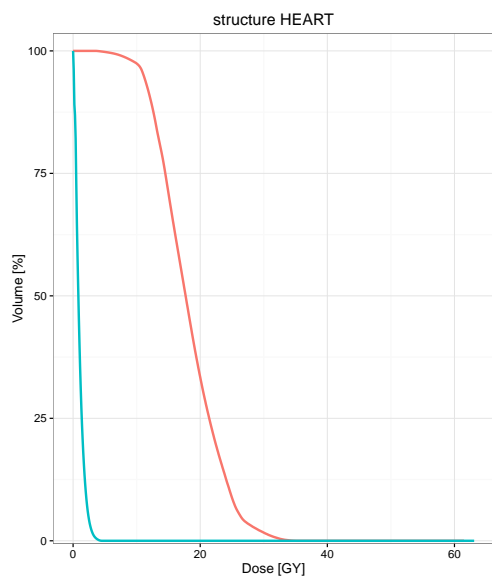
Cumulative as well as differential DVH diagrams can be generated with `showDVH()`. If you are using RStudio or Architect, all produced diagrams are accessible in the plots tab by clicking on the left and right arrows. Depending on the option `byPat`, each DVH diagram either shows one patient with multiple structures (`byPat=TRUE`) or one structure with multiple patients (`byPat=FALSE`).

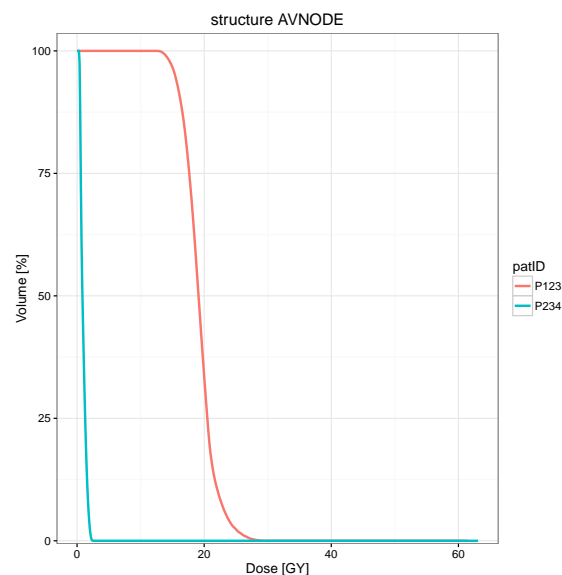
```
showDVH(dataMZ, byPat=TRUE)
```



Patient IDs and structures can be selected with the `patID="⟨ID⟩"` option and the `structure="⟨NAME⟩"` option. With `fixed=FALSE`, both accept regular expressions. By default, IDs and structure names are matched exactly. By default, all patients/structures are shown.

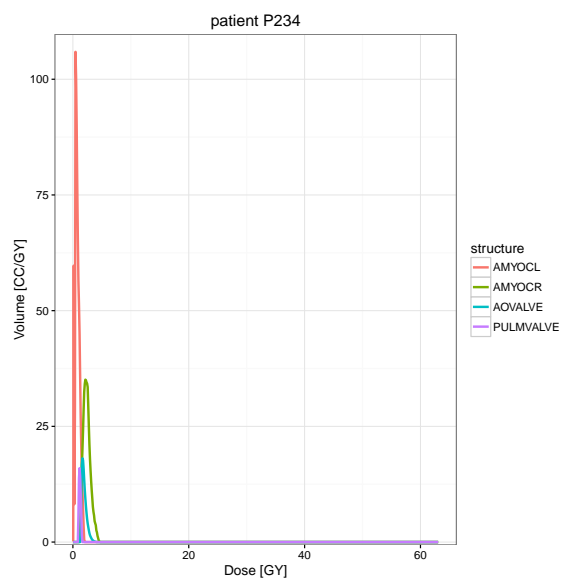
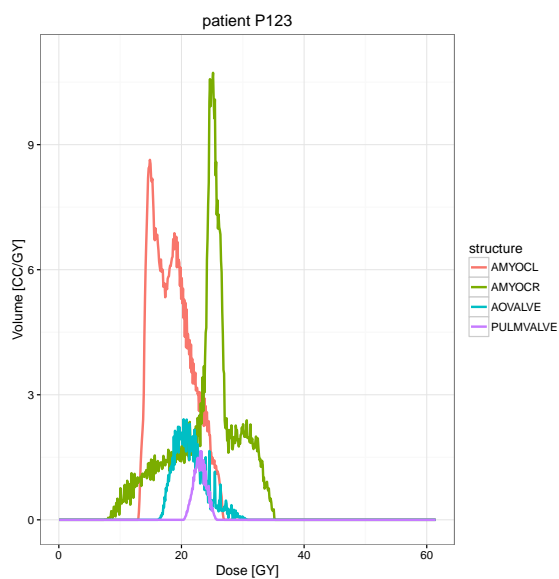
```
showDVH(dataMZ, byPat=FALSE, patID=c("P123", "P234"))
```

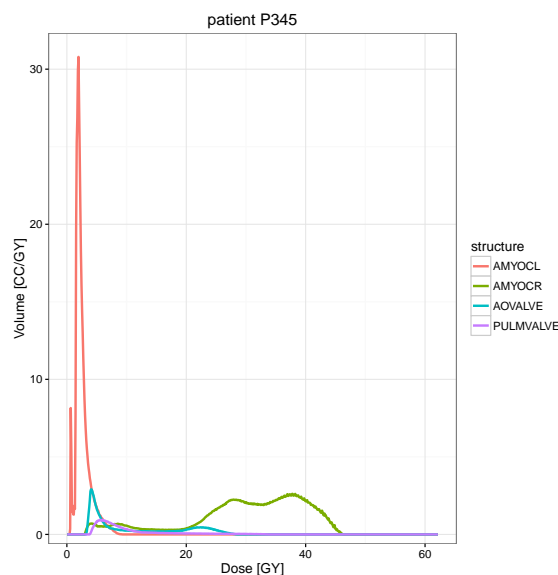




By default, the relative DVH is shown. Absolute volume (if available in the input files) can be plotted with the `rel=FALSE` option. For differential DVH, set `cumul=FALSE`.

```
# match structures containing "VALVE" and "AMYOC"
showDVH(dataMZ, cumul=FALSE, rel=FALSE,
        structure=c("VALVE", "AMYOC"), fixed=FALSE)
```



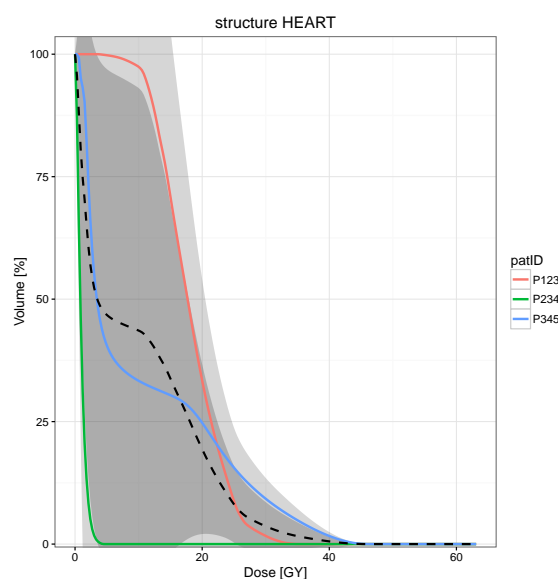


Option `thresh` allows to restrict the range of the x -axis such that only relative volumes larger than `thresh` appear. Use option `show=FALSE` to prevent the diagrams from being shown if you just need the returned object (here: `dvhPlot`) to later save the diagrams to file.

```
# just save the diagram but don't show it
dvhPlot <- showDVH(dataMZ, structure=c("HEART", "AOVALVE", "AVNODE"),
  rel=FALSE, thresh=0.001, show=FALSE)
```

With option `addMSD=TRUE`, the diagram also shows the point-wise mean DVH as a black curve as well as grey shaded areas for the regions defined by the point-wise 1 standard deviation and 2 standard deviations around this mean (see section 4.4). With `byPat=FALSE` and `addMSD=TRUE`, the average DVH for one structure over many patients can be visually assessed.

```
# add point-wise mean DVH and 1 SD/2 SD regions
showDVH(dataMZ, structure="HEART", byPat=FALSE, addMSD=TRUE)
```



5.2 Save cumulative DVH diagrams to file

DVH diagrams can be saved to file using `saveDVH()`. A file name pattern can then be supplied to option `file`. By using different file extensions like `.pdf`, `.jpg`, `.png`, different graphics formats can be automatically selected. In addition, the width and height of the diagram can be specified in inch.

```
saveDVH(dvhPlot, file="c:/folder/dvh.pdf", width=7, height=5)
```

6 Quality assurance constraints on the dose-volume relationship

For quality assurance, it is possible to define, check, and visualize constraints on the dose-volume relationship for DVHs.

6.1 Define constraints

A DVH constraint is a character string that consists of three parts: The DVH metric (see section 4.1), a comparison operator among `<`, `>`, `<=`, `>=`, and the reference value together with the measurement unit – one among `Gy`, `cGy`, `cc`, `%`. For constraints involving the relative dose, the DVH must contain the prescription dose.

Some example constraints are `"V10Gy > 80%"` (more than 80% of the structure should have received 10Gy), `"V20% < 10CC"` (less than 10cm³ of the structure should have received 20% of the prescription dose), or `"D10CC > 500cGy"` (The “hottest” 10cm³ of the structure should have received more than 500cGy). Constraints can also apply to the dose mean, median, and standard deviation as well as to the gEUD and to the (N)TCP.

A DVH constraint can apply to a specific patient or to all patients, and to a specific structure or to all structures.

- If constraints apply to all patients/structures, the constraint can be a **character** vector with elements like the examples above.
- If constraints apply only to some patients/structures, the constraint must be a data frame with variables **constraint**, **patID** and **structure**. Each row then defines one constraint and its scope: **constraint** must be a character string with one constraint definition as in the examples above. **patID** must be either a character string with a valid patient ID, or `"*"` if the constraint applies to all patients. **structure** must be either a character string with a valid structure name, or `"*"` if the constraint applies to all structures. If variable **patID** is missing from the data frame, the constraints apply to all available patients. If variable **structure** is missing from the data frame, the constraints apply to all available structures.

Alternatively, it is possible to specify a set of constraints as a table in a text file with one row per constraint and one column for the constraint expression, structure, and patient ID. A table like this can be created in a spreadsheet program like Excel (fig. 1), be exported to a tab-delimited text-file, and be read in by function `readConstraints()`. Table 2 shows some examples.

```
dataConstr <- readConstraints("constraints.txt", dec=".", sep="\t")
```


Table 2: Example for pasted constraints.

Constraints that apply to all patients and to all structures

```
"D10cc < 20%"
"V5cGy > 100cc"
"DMEAN < 10Gy"
```

Constraints that apply to some patients and to all structures

"constraint"	"patID"
"D10cc < 20%"	"P123"
"V5cGy > 100cc"	"*"
"DMEAN < 10Gy"	"P234"

Constraints that apply to some patients and to some structures

"constraint"	"patID"	"structure"
"D10cc < 20%"	"P123"	"*"
"V5cGy > 100cc"	"*"	"HEART"
"DMEAN < 10Gy"	"P234"	"AOVALVE"

The constraint data frame `dataConstr` is built into `DVHmetrics` and applies to the `dataMZ` DVH data.

```
dataConstr      # show defined constraints and their scope
```

	constraint	structure	patID
1	V1.2Gy> 60%	AVNODE	P123
2	V10Gy_cc < 18 cc	AMOYCL	P123
3	D80% < 1.8Gy	AOVALVE	P234
4	D200cc >2%	HEART	P234
5	V4% > 25%	HEART	P345
6	V7.5Gy< 10%	HEART	P345

For checking constraints, and for calculating the difference between the observed DVH and the constraint, the DVH is linearly interpolated, by using monotone Hermite splines, or by local polynomial kernel regression.

6.2 Check constraints

Constraints are checked with `checkConstraint()`. The output returns information on the observed value of the tested metric, on the compliance with respect to this metric, and on the absolute/relative deviation in volume as well as in dose to the specified constraint value. The units for the absolute deviation are those used in the constraint expression. When the constraint defines a point in dose-volume space, `checkConstraint()` reports another quantitative measure for the degree of violation: The closest point on the DVH to the constraint as well as its Euclidean distance to the constraint point.

For calculating the minimal Euclidean distance between the constraint point and the DVH, the constraint point is orthogonally projected onto each DVH segment between (interpolated) DVH nodes.

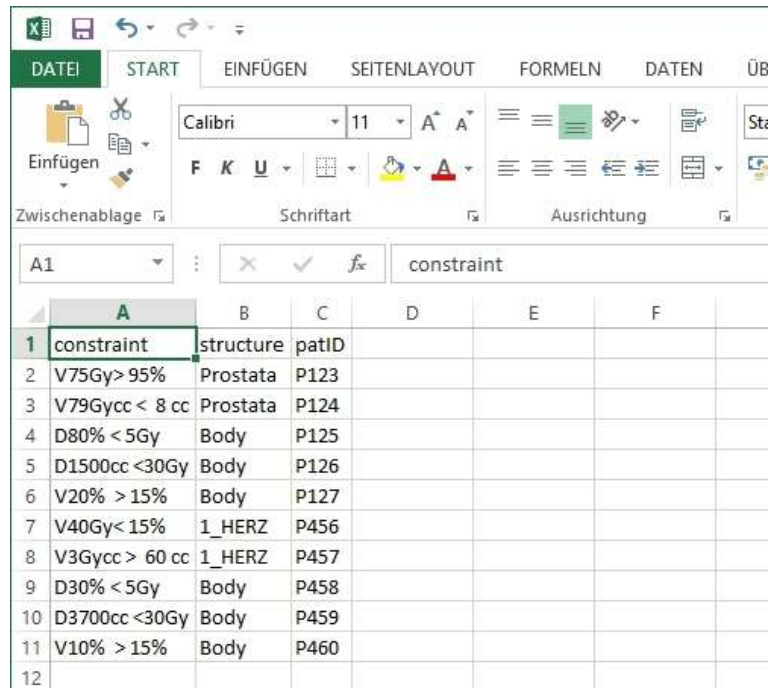


Figure 1: Defining constraints in a spreadsheet program like Excel

The relative Euclidean distance is the minimum of these distances divided by the distance of the constraint point to the closest axis (dose and volume) along the same direction. In doing so, the deviation from the expected volume per dose and the deviation from the expected dose per volume are condensed in a single metric.

As an example, we use the DVHs and corresponding constraints that are built into the DVHmetrics package.

```
## store result in object cc to save to file later
cc <- checkConstraint(dataMZ, constr=dataConstr)
print(cc, digits=2) # show output with 2 decimal places
```

	patID	structure	constraint	observed	compliance	deltaV	deltaVpc
1	P123	AVNODE	V1.2GY_% > 60%	100.0	TRUE	40	67
2	P234	AOVALVE	D80%_GY < 1.8GY	1.6	TRUE	-23	-29
3	P234	HEART	D200CC_% > 2%	2.2	TRUE	27	13
4	P345	HEART	V4%_% > 25%	66.2	TRUE	41	165
5	P345	HEART	V7.5GY_% < 10%	35.6	FALSE	26	256

	deltaD	deltaDpc	dstMin	dstMinRel	ptMinD	ptMinV
1	17.38	1448.4	17.35	1443.7	18.5	61
2	-0.20	-11.2	0.20	11.2	1.6	80
3	0.16	7.8	0.16	7.8	2.2	200
4	29.11	727.8	13.61	204.8	12.2	36
5	21.79	290.5	17.93	209.3	23.2	19

The result from a constraint check can be saved with function `saveConstraint()` that works like `saveMetric()` (see section 4.2).

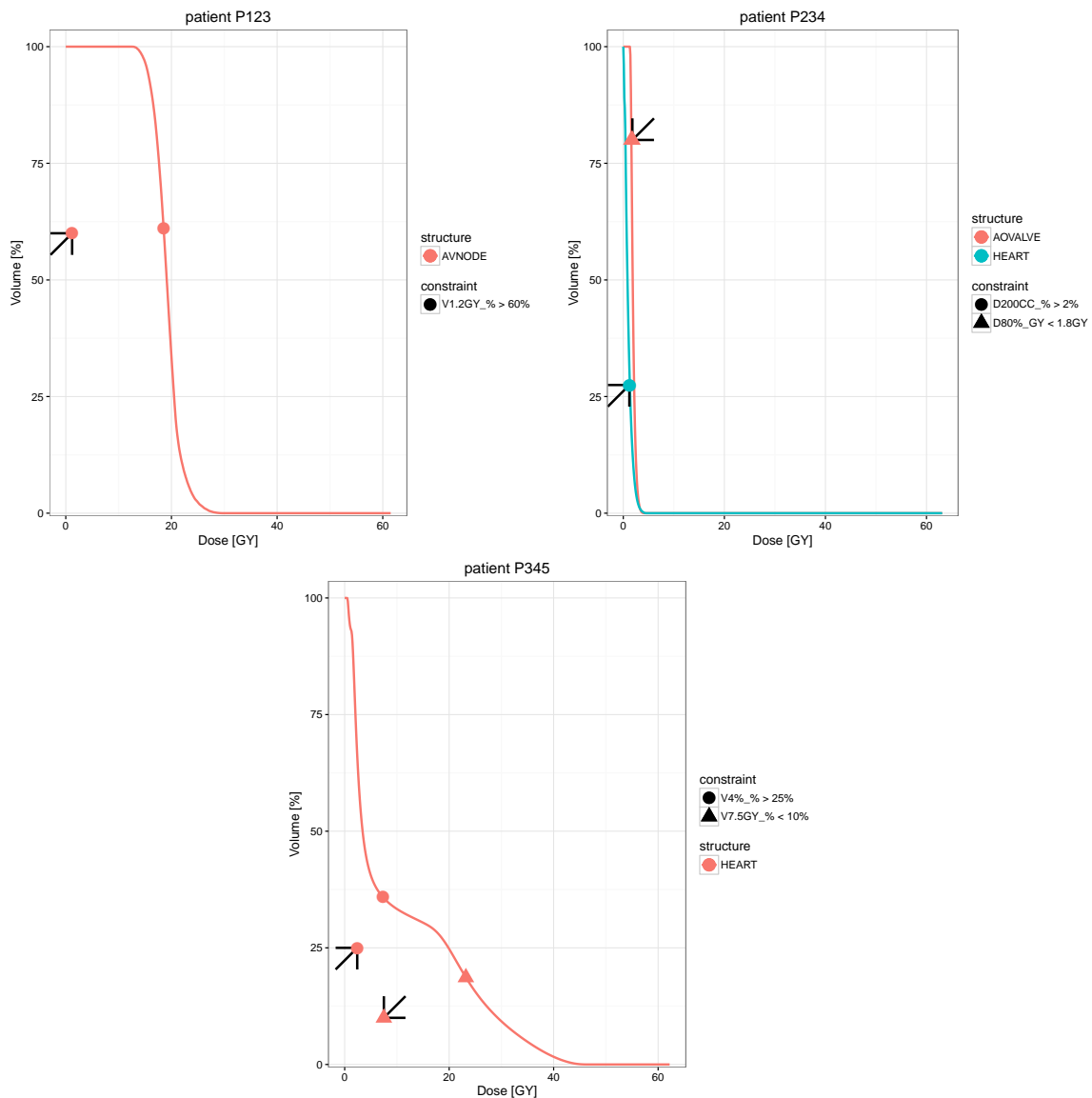
```
saveConstraint(cc, file="c:/folder/constrCheck.txt")
```

6.3 Visualize constraints

Constraints that define a point in dose-volume space can be visualized in a DVH with relative volume or absolute volume. The constraints will be converted to match the DVH plot. Only patients and structures within the scope of the defined constraints are shown. The diagram also shows the point on the DVH closest to the constraint. This can be verified visually only if the aspect ratio of the diagram is 1.

As in `showDVH()` (see section 5.1), either one diagram per patient with multiple structures is shown (`byPat=TRUE`), or one diagram per structure with multiple patients (`byPat=FALSE`).

```
## plot relative volume
showConstraint(dataMZ, constr=dataConstr, byPat=TRUE)
```



```
## plot absolute volume - store result in sc to save to file later
sc <- showConstraint(dataMZ, constr=dataConstr,
                     byPat=FALSE, rel=FALSE)
```

The result can be saved using `saveDVH()` as demonstrated in section 5.2.

```
saveDVH(sc, file="c:/folder/dvhConstraint.pdf")
```

7 BED, EQD2, Isoeffective Dose

The linear-quadratic model for the proportion of surviving cells S after dose d is (IAEA & ICRU, 2008):

$$S = e^{-(\alpha d + \beta d^2)}$$

According to the model, the biologically effective dose (BED) with total dose D , fraction dose d and a tissue-dependent α/β ratio is:

$$\text{BED} = D \left[1 + \frac{d}{\alpha/\beta} \right]$$

Given two different fractionation schemes, the total dose D_2 for the new fraction dose d_2 that corresponds to the total dose D_1 from the reference fraction dose d_1 can be calculated from solving the following equation for the desired measure:

$$\frac{D_2}{D_1} = \frac{d_1 + (\alpha/\beta)}{d_2 + (\alpha/\beta)}$$

As a special case, the dose in 2Gy fractions biologically equivalent dose (EQD₂) is given by:

$$\text{EQD}_2 = D_1 \cdot \frac{d_1 + (\alpha/\beta)}{2 + (\alpha/\beta)} = \frac{\text{BED}}{1 + \frac{2}{\alpha/\beta}}$$

The following convenience functions allow for easy calculation of these measures:

```
getBED(D=50, fd=2.5, ab=c(2, 3, 4))
```

```
      BED fractDose ab
1 112.50        2.5  2
2  91.67        2.5  3
3  81.25        2.5  4
```

```
getEQD2(D=50, fd=2.5, ab=c(2, 3, 4))
```

```

      EQD2 fractDose ab
1 56.25      2.5  2
2 55.00      2.5  3
3 54.17      2.5  4

getIsoEffD(D1=70, fd1=2, fd2=3, ab=c(3.5, 10))

[1] 59.23 64.62

```

The same functions can be used to convert complete DVHs to BED, EQD2, or to the iso-effective dose corresponding to some other fraction dose.

```

getEQD2(D=dataMZ[[c(1, 1)]], fd=2.5, ab=3)

DVH: Patient 'John Doe' (ID P123), structure 'HEART' (600 CC), Dose: 0.11-68GY

```

Acknowledgements

The authors thank Marcus Stockinger for ideas on checking quality assurance constraints as well as Sandra Bührdel, Hannes Rennau, Ulrich Wolf, Bjorne Riis, Nico Banz, and Michael R. Young for example DVH files exported from different treatment planning systems.

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