

Package ‘multisensi’

May 20, 2010

Type Package

Title Multivariate Sensitivity Analysis

Version 1.0-3

Date 2010-05-20

Author Matieyendou LAMBONI <clamboni@yahoo.fr>, Herve MONOD
<herve.monod@jouy.inra.fr>

Maintainer Herve MONOD <herve.monod@jouy.inra.fr>

Description An R library for performing sensitivity analysis on a model with multivariate output

License CeCILL-2

Repository CRAN

LazyLoad yes

Depends R (>= 2.8.0)

Suggests MASS

R topics documented:

multisensi-package	2
acp	3
anoasg	4
anovadec	4
asg	5
biomasse	6
Climat	7
dynsi	8
graph.bar	9
graph.pc	10
grpe.gsi	11
gsi	11
plan	13
planfact	14
planfact.as	14
plot.dynsi	15

plot.gsi	15
print.dynsi	16
print.gsi	17
quality	17
simulmodel	18
summary.dynsi	19
summary.gsi	19
yapprox	20
Index	21

multisensi-package *Multivariate sensitivity Analysis*

Description

Sensitivity Analysis (SA) for models with multivariate output

Details

This package contains three methods for performing sensitivity analysis on simulation models with multivariate output:

- i) `gsi` function for the Generalised Sensitivity Analysis (Lamboni et al., 2009) based on inertia decomposition. This method synthesizes the information that is spread between the time outputs or between the principal components and produces a unique sensitivity index for each factor.
- ii) `gsi` function for the componentwise sensitivity analysis obtained by computing sensitivity indices on principal components (Campbell et al., 2006)
- iii) `dynsi` function for the dynamic sensitivity analysis obtained by computing sensitivity indices on each output variable.

For all three methods, sensitivity indices are calculated presently by using a factorial design and a classical ANOVA decomposition.

Simulation model management

The multisensi package works on simulation models coded either in **R** or using an external language (typically as an executable file). Models coded in **R** must be either functions or objects that have a predict method, such as `lm` objects. Models defined as functions will be called once with an expression of the form $y \leftarrow f(X)$ where X is a vector containing a combination of levels of the input factors, and y is the output vector of length q , where q is the number of output variables. If the model is external to **R**, for instance a computational code, it must be analyzed with the decoupled approach: the methods require an input data frame (X) containing all the combinations of the input levels and the outputs data frame (Y) containing the response of the model corresponding to these combinations. The size of X is $n * p$ and the size of Y is $n * q$ where p is the number of the input factor, q is the number of the model outputs and n is the number of all the combinations of the input levels. This approach can also be used on **R** models that do not fit the required specifications.

Author(s)

Matieyendou Lamboni <clamboni@yahoo.fr>, Hervé Monod <herve.monod@jouy.inra.fr>

References

- Lamboni, M., Makowski, D., Monod, H., 2009. Multivariate global sensitivity analysis for dynamic crop models. *Field Crops Research*, volume 113. pp. 312-320
- Lamboni, M., Makowski, D., Monod, H., 2009. Multivariate sensitivity analysis to measure global contribution of input factors in dynamic models (submitted in october 2009 to *Reliability Engineering \& System Safety*)
- Saltelli, A., Chan, K., Scott, E.M. eds, 2000. *Sensitivity Analysis* Wiley, New York.

acp

Principal Component Analysis (PCA)

Description

Principal Component Analysis (PCA) for the generalized sensitivity analysis

Usage

```
ACP(simuls, normalized = TRUE)
```

Arguments

<code>simuls</code>	data frame, typically a multivariate model output
<code>normalized</code>	If TRUE, a normalized PCA is performed

Value

an object of class `prcomp`; see the `prcomp` help for further details

Note

This is essentially an internal function for the `multisensi` package

Author(s)

M. LAMBONI

See Also

`prcomp`

anoasg

Dynamic main and total sensitivity indices

Description

Function to compute the main and total dynamic sensitivity indices

Usage

```
anoasg(ANO, nbcomp = 2)
```

Arguments

ANO	anova object obtained from the anovadec function
nbcomp	number of model output to be considered

Value

A list with the following components:

SI data frame of first order, second order, ... indices

tSI data frame of total sensitivity

mSI data frame of main sensitivity indices

iSI data frame of interaction sensitivity indices

indic.fact data frame of anova object attribute

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

anovadec

Computation of several anovas on the output of a PCA

Description

A function to compute sum of squares decomposition on principal components by using the aov function

Usage

```
anovadec(ACP, plan, ord.inter, nbcomp = 2)
```

Arguments

ACP	data.frame of model output, usually the x component of a PCA object
plan	data.frame of input design
ord.inter	ANOVA formula like "A+B+C+A:B" OR an integer giving the maximum interaction order (1 for main effects)
nbcomp	number of principal components to be considered (e.g 3)

Value

The anovadec function returns a two-component list:

aov list of AOV objects

PC prediction of output

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

See Also

aov

asg

Main and total generalized sensitivity computation

Description

Function to compute the main and total generalized sensitivity indices

Usage

```
asg(ANO, ACP, sigma.car, nbcomp = 2)
```

Arguments

ANO	ANOVA Object obtained from anovadec function
ACP	ACP object
sigma.car	Inertia for the model output
nbcomp	Numbers of principal component (PC) to be considered

Value

A list with the following components:

SI data frame of first order, second order, ... indices

mSI data frame of main sensitivity indices

tSI data frame of total sensitivity

iSI data frame of interaction sensitivity indices

cor data frame of correlation between PCs and model output

inertia Vector of Inertia explained by PCs

indic.fact data frame of anova object attribute

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

biomasse

The Winter Wheat Dynamic Model

Description

The Winter Wheat Dynamic Model, a toy model to illustrate the main multisensi methods

Usage

```
biomasse(input, climdata, annee = 3)
```

Arguments

input vector of input value

annee year

climdata a meteorological data.frame specific to biomasse

Details

The Winter Wheat Dry Matter model (WWDm) is a dynamic crop model running at a daily time step (Makowski et al, 2004). It has two state variables, the above-ground winter wheat dry matter $U(t)$, in g/m^2 and the leaf area index $LAI(t)$ with t the day number from sowing ($t = 1$) to harvest ($t = 223$). In the multisensi-package implementation, the `biomasse` function simulates the output for only one parameter set (the first row of `input` if it is a matrix or a data.frame).

Value

a vector of daily dry matter increase of the Winter Wheat biomass, over 223 days

Author(s)

initially Makowski, D., 2004

References

Makowski, D., Jeuffroy, M.-H., Gu\'erif, M., 2004 Bayesian methods for updating crop model predictions, applications for predicting biomass and grain protein content. In: Bayesian Statistics and Quality Modelling in the Agro-Food Production Chain (van Boekel et al. eds), pp. 57-68. Kluwer, Dordrecht

Monod, H., Naud, C., Makowski, D., 2006 Uncertainty and sensitivity analysis for crop models. In: Working with Dynamic Crop Models (Wallach D., Makowski D. and Jones J. eds), pp. 55-100. Elsevier, Amsterdam

Climat

Climate data

Description

Climate data for the WWDM model (needed by the `biomasse` function)

Usage

```
data(Climat)
```

Format

A data frame with 3126 observations on the following 4 variables.

`ANNEE` a factor with levels 1 to 14, indicating 14 different years

`RG` daily radiation variable

`Tmin` daily maximum temperature

`Tmax` daily minimum temperature

Source

Makowski, D., Jeuffroy, M.-H., Gu\'erif, M., 2004 Bayesian methods for updating crop model predictions, applications for predicting biomass and grain protein content. In: Bayesian Statistics and Quality Modelling in the Agro-Food Production Chain (van Boekel et al. eds), pp. 57-68. Kluwer, Dordrecht.

Monod, H., Naud, C., Makowski, D., 2006 Uncertainty and sensitivity analysis for crop models. In: Working with Dynamic Crop Models (Wallach D., Makowski D. and Jones J. eds), pp. 55-100. Elsevier, Amsterdam

Description

dynsi implements the Dynamic Sensitivity Indices. This method allows to compute classical Sensitivity Indices on each output variable of a dynamic or multivariate model by using the ANOVA decomposition

Usage

```
dynsi(formula, model, factors, cumul = FALSE, simulonly=FALSE,
      nb.outp = NULL, Name.File=NULL, ...)
```

Arguments

formula	ANOVA formula like "A+B+c+A:B" OR an integer equal to the maximum interaction order in the sensitivity model
model	output data.frame OR the name of the R-function which calculates the model output. The only argument of this function must be a vector containing the input factors values
factors	input data.frame (the design) if model is a data.frame OR a list of factors levels such as <code>factor.example <- list(A=c(0,1), B=c(0,1,4))</code>
cumul	logical value. If TRUE the sensitivity analysis will be done on the cumulative outputs
simulonly	logical value. If TRUE the program stops after calculating the design and the model outputs
nb.outp	The first nb.outp number of model outputs to be considered. If NULL all the outputs are considered
Name.File	optional name of a R script file containing the R-function that calculates the simulation model. e.g "exc.ssc"
...	possible fixed parameters of the model function

Details

If factors is a list of factors, the dynsi function generates a complete factorial design. If it is a data.frame, dynsi expects that each column is associated with an input factor.

Value

dynsi returns a list of class "dynsi", containing all the input arguments detailed before, plus the following components:

X	a data.frame containing the experimental design (input samples)
Y	a data.frame containing the output matrix (response)
SI	a data.frame containing the Sensitivity Indices (SI) on each output variable of the model
mSI	a data.frame of principal SI on each output variable

tSI a data.frame containing the total SI on each output variable
 iSI a data.frame of interaction SI on each output variable
 ...

Author(s)

Matieyendou LAMBONI

References

M. Lamboni, D. Makowski and H. Monod, 2009. Multivariate global sensitivity analysis for dynamic crop models. *Field Crops Research*, 113, 312-320.
 A. Saltelli, K. Chan and E. M. Scott eds, 2000. *Sensitivity Analysis*. Wiley, New York.

See Also

gsi

Examples

```
##---- Should be DIRECTLY executable !! ----
# Test case : the Winter Wheat Dynamic Models (WWDM)
# input factors design,
data(plan)
# input Climate variables
data(Climat)
DYNSI <- dynsi(2, biomasse, plan, nb.outp=10, climdata=Climat)
summary(DYNSI)
print(DYNSI)
plot(DYNSI)
#graph.bar(DYNSI,col=1, beside=F) # sensitivity bar plot
#                                # for the first output (col=1)
#graph.bar(DYNSI,col=2, xmax=1)  #
```

graph.bar

Sensitivity index bar plot

Description

A function that plots sensitivity indices by a bar graph

Usage

```
graph.bar(x, col = 1, nb.plot = 15, xmax = NULL, beside = TRUE, ...)
```

Arguments

<code>x</code>	an object of class <code>gsi</code> or <code>dynsi</code>
<code>col</code>	the column number of GSI to represent in the bar graph
<code>nb.plot</code>	number of input factors to be considered
<code>xmax</code>	a user-defined maximal x value ($x \leq 1$) in all the bar graphs that show sensitivity indices; or <code>NULL</code> if the user wants to keep default values
<code>beside</code>	if <code>TRUE</code> , the main and total sensitivity indices are represented by two bars; if <code>FALSE</code> , they are represented by the same bar
<code>...</code>	graphical parameters

Author(s)

M. LAMBONI

graph.pc

Principal Components graph for gsi objects

Description

A function that plots the Principal components (PCs) and the sensitivity index on each PC

Usage

```
graph.pc(x, nb.plot = 15, nb.comp = NULL, xmax = NULL,
         beside = TRUE, ...)
```

Arguments

<code>x</code>	gsi object
<code>nb.plot</code>	number of input factors to be considered
<code>nb.comp</code>	number of PCs
<code>xmax</code>	a user-defined maximal x value ($x \leq 1$) in all the bar graphs that show sensitivity indices; or <code>NULL</code> if the user wants to keep default values
<code>beside</code>	if <code>TRUE</code> , the main and total sensitivity indices are represented by two bars; if <code>FALSE</code> , they are represented by the same bar
<code>...</code>	graphical parameters

Author(s)

M. LAMBONI

grpe.gsi	<i>Group factor GSI, obsolete function</i>
----------	--

Description

An obsolete function that computed the GSI of a group factor as one factor

Usage

```
grpe.gsi(GSI, fact.interet)
```

Arguments

GSI a gsi or dynsi object
fact.interet input factor to be grouped

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

gsi	<i>Generalized Sensitivity Indices: GSI</i>
-----	---

Description

The gsi function implements the calculation of Generalised Sensitivity Indices. This method allows to compute a synthetic Sensitivity Index for the dynamic or multivariate models by using factorial designs and the MANOVA decomposition of inertia. It computes also the Sensitivity Indices on principal components

Usage

```
gsi(formula, model, factors, inertia = 0.95, normalized = TRUE,  
    cumul = FALSE, simulonly = FALSE, Name.File = NULL, ...)
```

Arguments

formula	ANOVA formula like "A+B+C+A:B" OR an integer equal to the maximum interaction order in the sensitivity model
model	output data.frame OR the name of the R-function which calculates the model output. The only argument of this function must be a vector containing the input factors values
factors	input data.frame (the design) if model is a data.frame OR a list of factors levels such as : <code>factor.example <- list(A=c(0,1), B=c(0,1,4))</code>

<code>inertia</code>	cumulated proportion of inertia (a scalar < 1) to be explained by the selected Principal components OR number of PCs to be used (e.g 3)
<code>normalized</code>	logical value. TRUE (default) computes a normalized Principal Component analysis.
<code>cumul</code>	logical value. If TRUE the PCA will be done on the cumulative outputs
<code>simulonly</code>	logical value. If TRUE the program stops after calculating the design and the model outputs
<code>Name.File</code>	optional name of a R script file containing the R-function that calculates the simulation model. e.g <code>"exc.ssc"</code>
<code>...</code>	possible fixed parameters of the model function

Details

If `factors` is a list of factors, the `gsi` function generates a complete factorial design. If it is a `data.frame`, `gsi` expects that each column is associated with an input factor.

Value

`gsi` returns a list of class "gsi", containing all the input arguments detailed before, plus the following components:

<code>X</code>	a <code>data.frame</code> containing the experimental design (input samples)
<code>Y</code>	a <code>data.frame</code> containing the output matrix (response)
<code>SI</code>	a <code>data.frame</code> containing the Sensitivity Indices (SI) on PCs and the Generalized SI (GSI)
<code>mSI</code>	a <code>data.frame</code> of first order SI on PCs and first order GSI
<code>tSI</code>	a <code>data.frame</code> containing the total SI on PCs and the total GSI
<code>iSI</code>	a <code>data.frame</code> of interaction SI on PCs and interaction GSI
<code>cor</code>	a <code>data.frame</code> of correlation between PCs and outputs
<code>inertia</code>	vector of inertia per PCs and global criterion
<code>Rsquare</code>	vector of dynamic coefficient of determination

Author(s)

M. Lamboni

References

- M. Lamboni, D. Makowski and H. Monod, 2009. Multivariate global sensitivity analysis for dynamic crop models. *Field Crops Research*, volume 113. pp. 312-320
- M. Lamboni, D. Makowski and H. Monod, 2009. Multivariate sensitivity analysis to measure global contribution of input factors in dynamic models. Submitted to *Reliability Engineering and System Safety*.

See Also

`dynsi`

Examples

```
##---- Should be DIRECTLY executable !! ----
# Test case : the Winter Wheat Dynamic Models (WWDM)
# input factors design
data(plan)
# input climate variable
data(Climat)
GSI <- gsi(2, biomasse, plan, inertia=3, normalized=TRUE, cumul=FALSE, climdata=Climat)
summary(GSI)
print(GSI)
plot(x=GSI, beside=FALSE)
#plot(GSI, nb.plot=4)           # the 'nb.plot' most influent factors
                                # are represented in the plots
#plot(GSI,nb.comp=2, xmax=1)    # nb.comp = number of principal components
#plot(GSI,nb.comp=3, graph=1)  # graph=1 for first figure; 2 for 2nd one
                                # and 3 for 3rd one; or 1:3 etc.
#graph.bar(GSI,col=1, beside=F) # sensitivity bar plot on the first PC
#graph.bar(GSI,col=2, xmax=1)  #
```

plan

*A factorial input design for the main example***Description**

Factorial design (resolution V) data for the 7 WWDM model input factors

Usage

```
data(plan)
```

Format

A data frame with 2187 observations on the following 7 variables.

Eb First WWDM input factor name

Eimax Second WWDM input factor name

K Third WWDM input factor name

Lmax Fourth WWDM input factor name

A Fifth WWDM input factor name

B Sixth WWDM input factor name

TI Seventh WWDM input factor name

See Also

[biomasse](#)

Examples

```
data(plan)
## maybe str(plan) ; plot(plan) ...
```

planfact	<i>Complete factorial design in lexical order</i>
----------	---

Description

Function that generates a complete factorial design in lexical order

Usage

```
planfact(nb.niv, make.factor = TRUE)
```

Arguments

nb.niv	vector containing the number of each input levels
make.factor	logical value. If TRUE the columns of the output are of class factor

Value

plan	data frame of the complete factorial design
------	---

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

planfact.as	<i>Complete factorial design</i>
-------------	----------------------------------

Description

Computation of a complete factorial design for model input factors

Usage

```
planfact.as(input)
```

Arguments

input	list of factor levels
-------	-----------------------

Value

comp2	complete factorial design of model input
-------	--

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

plot.dynsi	<i>Plot method for dynamic sensitivity results</i>
------------	--

Description

Plot method for dynamic sensitivity results of class dynsi

Usage

```
## S3 method for class 'dynsi':
plot(x, text.tuning = NULL, ...)
```

Arguments

x	a dynsi object
text.tuning	NULL or a small integer to improve the position of input factor labels
...	graphical parameters

Details

For labels that would be partly positioned outside the plot frame, the argument "text.tuning" may allow to get a better positioning. If it is equal to n , say, these labels are moved by n positions inside the frame, where 1 position corresponds to 1 output variable on the x-axis.

Author(s)

M. LAMBONI

See Also[dynsi](#)

plot.gsi	<i>Plot method for generalised sensitivity analysis</i>
----------	---

Description

Plot method for generalised sensitivity analysis of class gsi

Usage

```
## S3 method for class 'gsi':
plot(x, nb.plot = 10, nb.comp = 3, graph = 1:3, xmax=NULL,
      beside=TRUE, ...)
```

Arguments

<code>x</code>	a gsi object
<code>nb.plot</code>	number of input factors to be considered
<code>nb.comp</code>	number of Principal Components to be plotted
<code>graph</code>	figures number: 1 or 2 or 3
<code>xmax</code>	a user-defined maximal x value ($x \leq 1$) in all the bar graphs that show sensitivity indices; or NULL if the user wants to keep default values
<code>beside</code>	if TRUE, the main and total sensitivity indices are represented by two bars; if FALSE, they are represented by the same bar
<code>...</code>	graphical parameters

Author(s)

M. LAMBONI

See Also[gsi](#)

`print.dynsi`*print DYNsi*

Description

A function to print DYNsi results

Usage

```
## S3 method for class 'dynsi':
print(x, ...)
```

Arguments

<code>x</code>	a dynsi object
<code>...</code>	print parameters

Author(s)

M. LAMBONI

See Also[dynsi](#)

print.gsi	<i>print GSI</i>
-----------	------------------

Description

function to print GSI results

Usage

```
## S3 method for class 'gsi':
print(x, ...)
```

Arguments

x	a gsi object
...	print parameters

Author(s)

M. LAMBONI

See Also

[gsi](#)

quality	<i>quality of any approximation</i>
---------	-------------------------------------

Description

Function that computes the sensitivity quality after making some assumptions about the number of PCs and the number of interactions

Usage

```
quality(echsimul, echsimul.app, normalise = TRUE)
```

Arguments

echsimul	model outputs
echsimul.app	Predicted model output
normalise	logical value

Value

A list with the following components:

moy mean

biais biais

coef.det R-square

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

simulmodel

Model simulation

Description

Function that simulates the model outputs

Usage

```
simulmodel(model, plan, nomFic = NULL, verbose = FALSE, ...)
```

Arguments

model	name of R-function
plan	data frame of input design
nomFic	name of file that contains the model function
verbose	verbose
...	... possible fixed parameters of the R-function

Details

The model function must be a R-functions. Models defined as functions will be called once with an expression of the form $\mathbf{y} \leftarrow \mathbf{f}(\mathbf{X})$ where \mathbf{X} is a vector containing a combination of levels of the input factors, and \mathbf{y} is the output vector of length q , where q is the number of output variables

Value

data frame of model outputs

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

summary.dynsi	<i>dynsi summary</i>
---------------	----------------------

Description

Function to summarize the dynamic sensitivity results

Usage

```
## S3 method for class 'dynsi':  
summary(object, ...)
```

Arguments

object	a dynsi object
...	summary parameters

Author(s)

M. LAMBONI

See Also

[dynsi](#)

summary.gsi	<i>summary of GSI results</i>
-------------	-------------------------------

Description

function to summarize the GSI results

Usage

```
## S3 method for class 'gsi':  
summary(object, ...)
```

Arguments

object	a GSI object
...	summary parameters

Author(s)

M. LAMBONI

See Also

[gsi](#)

yapprox

Prediction based on PCA and anovas

Description

A function that predicts the model output after PCA and aov analyses

Usage

```
yapprox(ACP, nbcomp = 2, aov.obj)
```

Arguments

ACP	prcomp object
nbcomp	number of PCs
aov.obj	aov object

Value

A list with components

Y model output predictions

trace model output inertia

Note

This is essentially an internal function for the multisensi package

Author(s)

M. LAMBONI

Index

*Topic **datasets**

Climat, [7](#)

plan, [12](#)

ACP (*acp*), [2](#)

acp, [2](#)

anoasg, [3](#)

anovadec, [4](#)

asg, [5](#)

biomasse, [6](#), [13](#)

Climat, [7](#)

dynsi, [2](#), [7](#), [15](#), [16](#), [18](#)

graph.bar, [9](#)

graph.pc, [10](#)

grpe.gsi, [10](#)

gsi, [2](#), [11](#), [15](#), [16](#), [19](#)

multisensi (*multisensi-package*), [1](#)

multisensi-package, [1](#)

plan, [12](#)

planfact, [13](#)

planfact.as, [14](#)

plot.dynsi, [14](#)

plot.gsi, [15](#)

print.dynsi, [16](#)

print.gsi, [16](#)

quality, [17](#)

simulmodel, [17](#)

summary.dynsi, [18](#)

summary.gsi, [19](#)

yapprox, [19](#)